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In Reliable, the delay may be chosen

to the number of users. In th

round with few arrivals (low traffic)

Our conclusion is that

way. The time stamp that determine how long a message should be held by an
E-G

A Method to compute the anonymity of Relialle

To formalize the behavior of the mixer, we define:

- X_s : an incoming message arriving at time s ;
- Y_t : an outgoing message leaving at time t ;
- D : the amount of time a message has been delayed.

We know that the mixer delays the message exponentially and we have set the mean to 1 hour: $D \sim \exp(1)$:

$$\begin{aligned} \text{pdf: } f(d) &= e^{-d} && \text{for all } d \geq 0 ; \\ &= 0 && \text{elsewhere ;} \\ \text{cdf: } F(d) &= P(D \leq d) = 1 - e^{-d} && \text{for all } d \geq 0 ; \\ &= 0 && \text{elsewhere .} \end{aligned}$$

All delay times are independent.

It is crucial to note in this setup that the sequence of outgoing messages is not a Poisson process. This would only be true if all input messages would arrive at the same time, hence belong to the mix when they

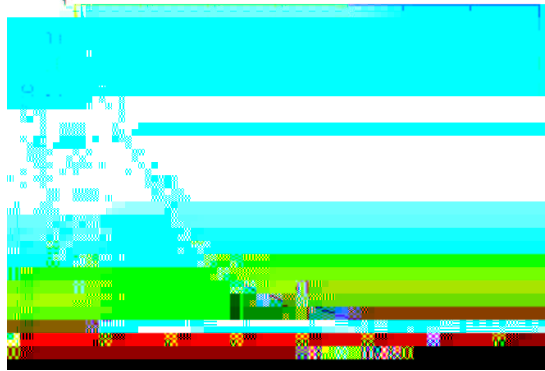


Fig. 9. An example of an exponential probability density function

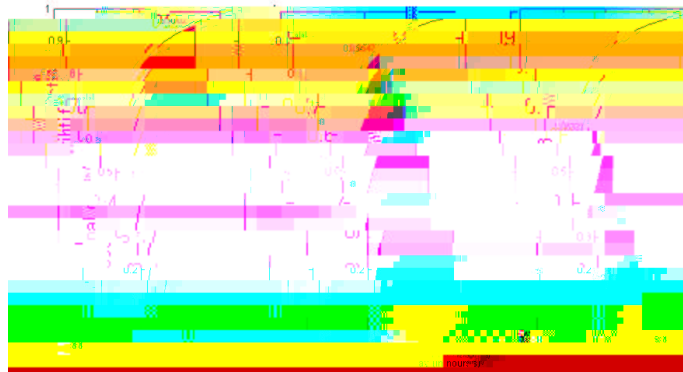


Fig. 10. The matching exponential cumulative density function

How can we then calculate the probabilities of the delay time? To make this clear, let us look at Figure 9 and suppose that we only have three arrival times prior to *out*. We have thus three possible delays $d_1 > d_2 > d_3$. Let us now assume for simplicity reasons that $d_1 = 3$ hours, $d_2 = 2$ hours and $d_3 = 1$ hour. The variable delay is continuous and can theoretically take any value between

in Figure 10

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